

## Interconnections and Linkages (Sec. 4.3)

Connections between bodies constrain their motion

constraint equations - kinematical representation of the constraints

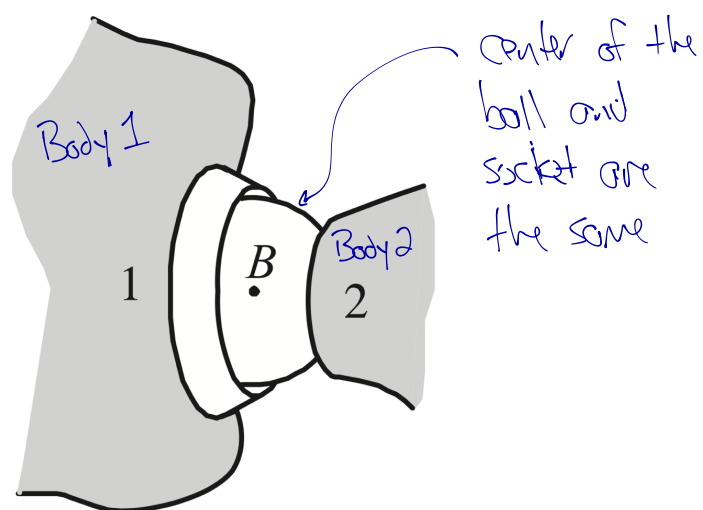
constraint forces or reactions - impose/enforce constraints

One common simplifying constraint is enforcing planar motion.

Q: To maintain planar motion, what must be true about angular velocity?

$\bar{\omega} \perp$  plane of motion to maintain motion only in that plane

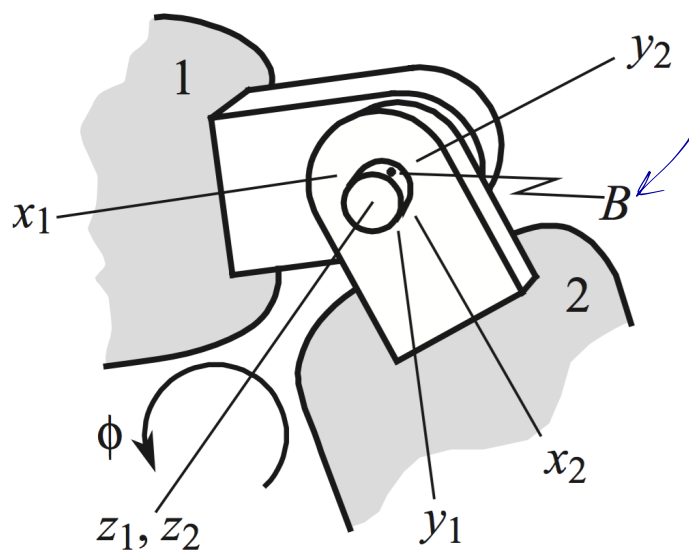
### Ball-and-socket Joints



$$\bar{v}_{B1} = \bar{v}_{B2} \quad \text{and} \quad \bar{a}_{B1} = \bar{a}_{B2}$$

Because B moves identically on bodies 1 and 2, the velocity and accel. must be equal.

### Pin Connections



Point B is shared between the bodies

$$\textcircled{1} \quad \bar{v}_{B1} = \bar{v}_{B2} \quad \text{and} \quad \bar{a}_{B1} = \bar{a}_{B2}$$

② Also a constraint on rotation

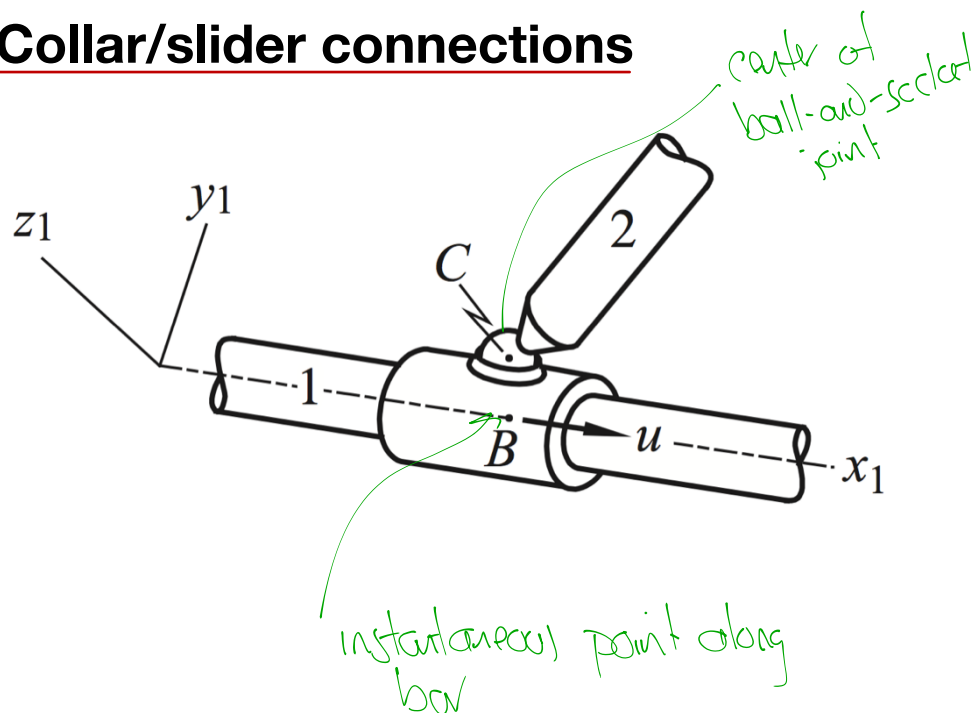
$$\bar{\omega}_2 = \bar{\omega}_1 + \dot{\phi} \bar{k}_1$$

and

$$\bar{\alpha}_2 = \bar{\alpha}_1 + \ddot{\phi} \bar{k}_1 + \dot{\phi} (\bar{\omega}_1 \times \bar{k}_1)$$

## Interconnections and Linkages (cont.)

### Collar/slider connections



Assume  $\bar{r}_{C/B} \approx 0$

collar moves in  $x_1$  direction

Let  $\dot{u}$  = relative velocity of the slider

$$(\bar{v}_C)_{x_1, y_1, z_1} = \dot{u} \bar{z}_1$$

$$\text{So, } \bar{v}_C = \bar{v}_B + \dot{u} \bar{z}_1 \quad \text{and} \quad \bar{a}_C = \bar{a}_B + \ddot{u} \bar{z}_1 + 2\bar{\omega}_1 \times \dot{u} \bar{z}_1$$

The collar could also be connected to the slider by a pin or clevis, which add additional constraints. See the book for more

Fully constrained system - = number of kinematic variables and equations

Partially constrained - number of kinematical variables exceeds number of kinematic eq.  
· number of "extra" variables = # of degrees-of-freedom.